



Classical trajectory perspective on double ionization
dynamics of atoms and molecules irradiated
by ultrashort intense laser pulses

Jie Liu (刘杰), Di-Fa Ye (叶地发)

Institute of Applied Physics and
Computational Mathematics (IAPCM),
Beijing, China

Thanks



Collaborators:

Prof. Jing Chen &
Prof. Li-Bin Fu

from the Institute of Applied Physics and
Computational Mathematics (IAPCM), Beijing

Prof. Xiao-Jun Liu

from the Wuhan Institute of Physics and
Mathematics (WIPM), Wuhan

Financial supports:

National Natural Science Foundation of China
No.10725521;

National Fundamental Research Programme of China
No.2006CB806000, 2006CB921400, 2007CB814800

CAEP Foundation
No. 2006Z0202.

Outline of the talk



☆ History review

☆ Newest experimental developments

☆ Difficulty of the existing theories

☆ Our semi-classical model

New!

☆ Explanation of the experiments

☆ Future perspective

☆ Conclusion

1. J. Liu, D. F. Ye, J. Chen, X. Liu,
Phys. Rev. Lett. 99, 013003 (2007)
2. D. F. Ye, J. Chen, J. Liu,
Phys. Rev. A 77, 013403 (2008)
3. D. F. Ye, X. Liu, J. Liu,
arXiv:0802.0041 (2008)

History review1994

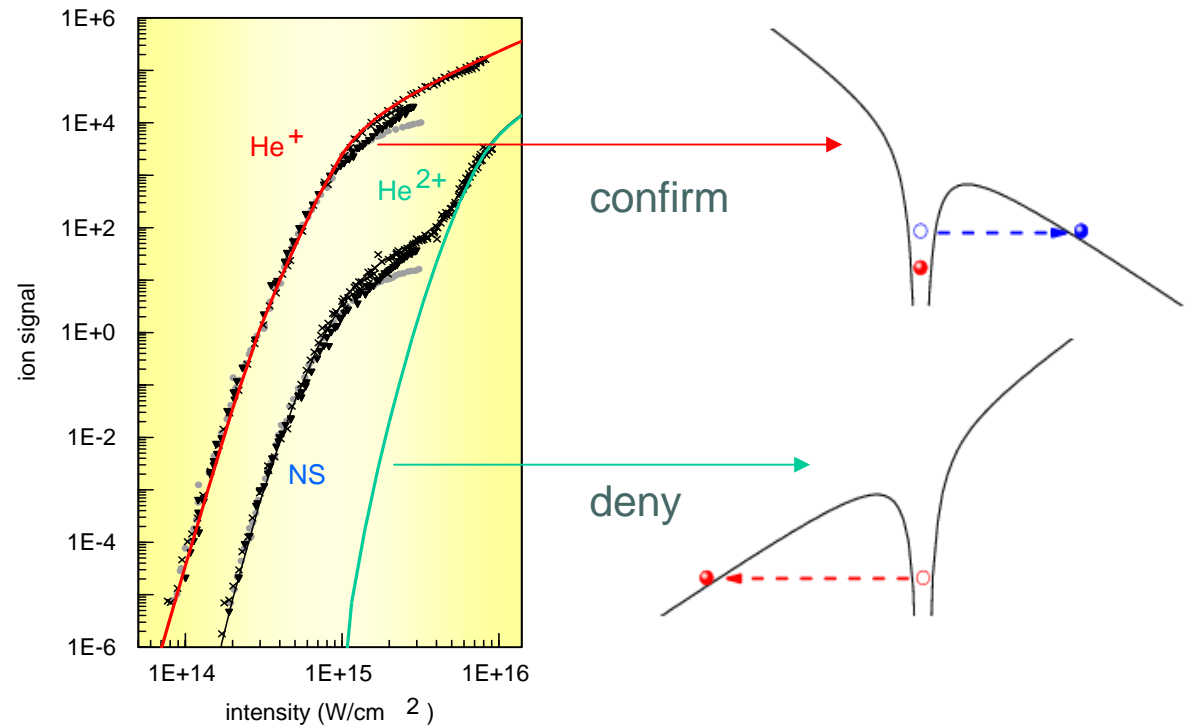


Single ionization
ADK theory ✓

Double ionization
No!

Experiments in the early 1990s showed considerably more double ionization than predicted by independent-electron model.

Electron correlation should be take into account !



B. Walker et al, Phys. Rev. Lett. 73, 1227 (1994)

History review2000



Direct evidence of electron correlation

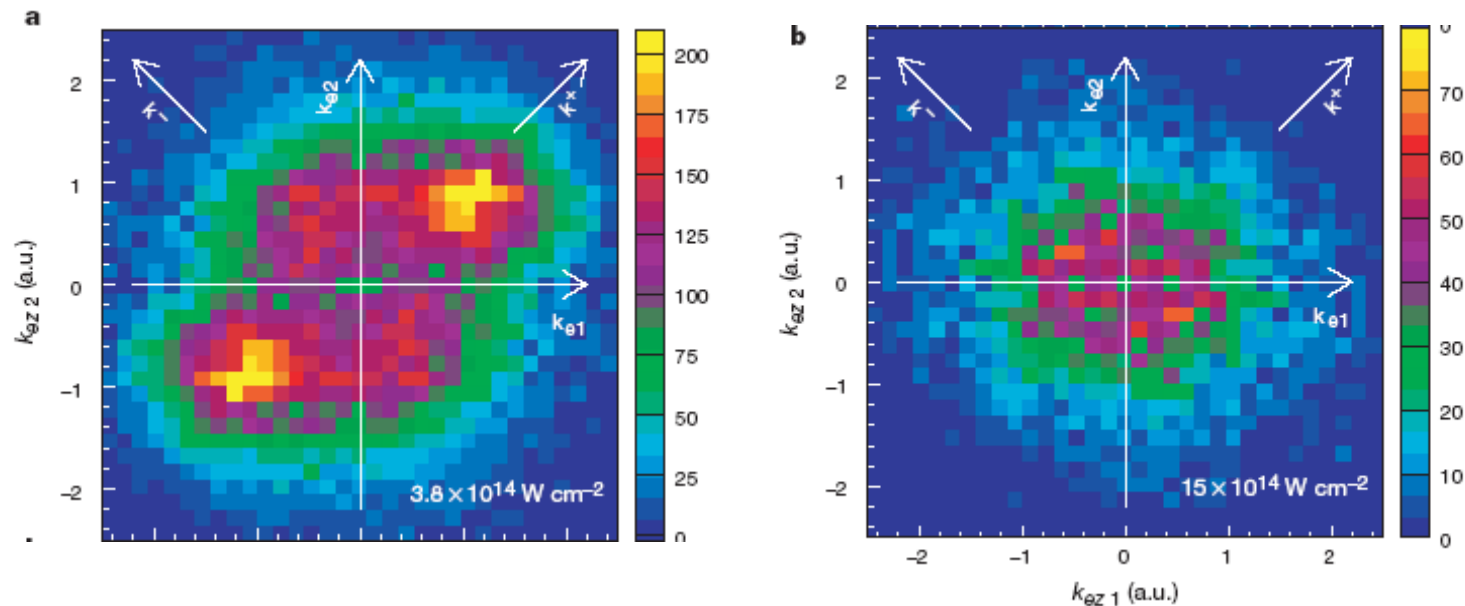


Figure 2 Momentum correlation between the two emitted electrons when an Ar^{2+} ion is produced in the focus of a 220-fs, 800-nm laser pulse at peak intensities of $3.8 \times 10^{14} \text{ W cm}^{-2}$ (a) and $15 \times 10^{14} \text{ W cm}^{-2}$ (b). The horizontal axis shows the momentum component of one electron along the polarization of the laser field; the vertical axis shows the same momentum component of the corresponding second electron. The same sign of the momenta for both electrons means emission to the same half sphere. The data are integrated over the momentum components in the direction perpendicular to the polarization. The colour coding shows the differential rate in arbitrary units.

History reviewlast day in 2007



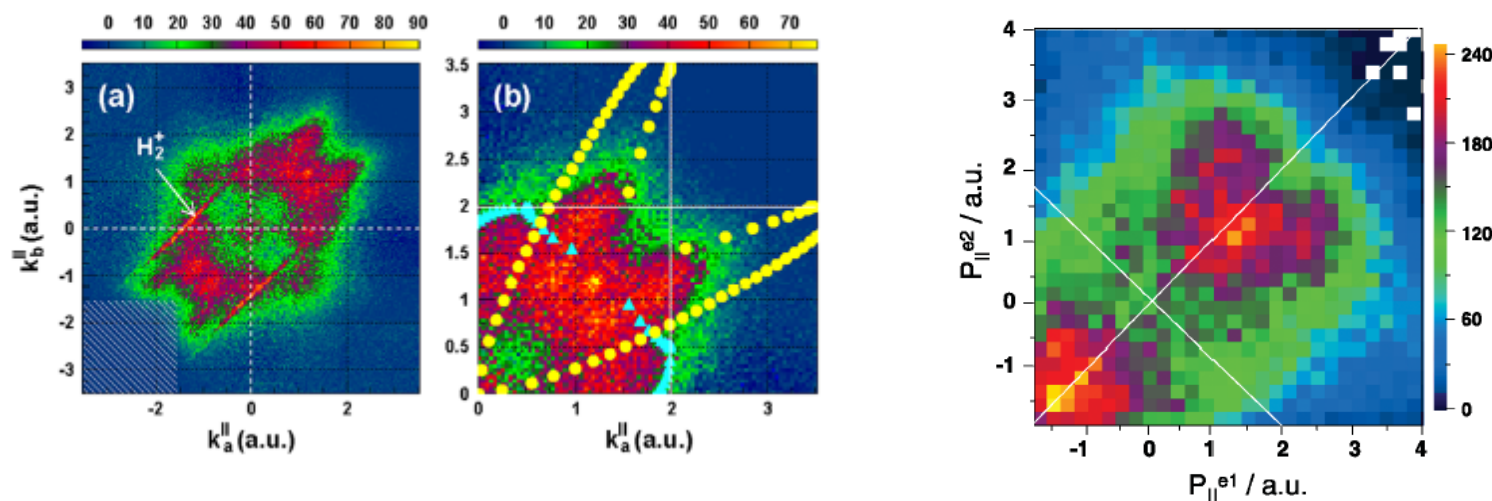
PRL 99, 263002 (2007)

PHYSICAL REVIEW LETTERS

week ending
31 DECEMBER 2007

Binary and Recoil Collisions in Strong Field Double Ionization of Helium

A. Staudte,^{1,*} C. Ruiz,² M. Schöffler,³ S. Schössler,³ D. Zeidler,⁴ Th. Weber,⁵ M. Meckel,³ D. M. Villeneuve,¹
P. B. Corkum,¹ A. Becker,² and R. Dörner³



PRL 99, 263003 (2007)

PHYSICAL REVIEW LETTERS

week ending
31 DECEMBER 2007

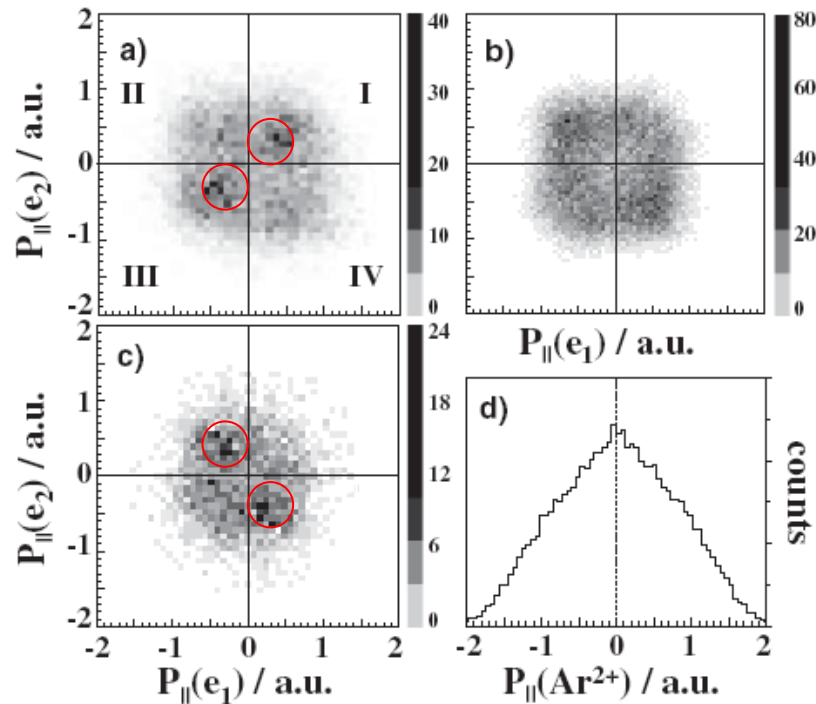
Correlated Two-Electron Momentum Spectra for Strong-Field Nonsequential Double Ionization of He at 800 nm

A. Rudenko,¹ V. L. B. de Jesus,² Th. Ergler,¹ K. Zrost,¹ B. Feuerstein,¹ C. D. Schröter,¹ R. Moshhammer,¹ and J. Ullrich¹



Strong-Field Double Ionization of Ar below the Recollision Threshold

Yunquan Liu,¹ S. Tschuch,¹ A. Rudenko,¹ M. Dürer,¹ M. Siegel,² U. Morgner,² R. Moshhammer,¹ and J. Ullrich¹







Back-to-Back emission
dominates

when the laser field is so weak that even the most energetic electron with maximum returned energy $3.17U_p$ can not directly free the inner electron.

FIG. 2. Correlated longitudinal momentum spectra $P_{\parallel}(e_1)$ vs $P_{\parallel}(e_2)$ for Ar double ionization. (a) 9×10^{13} W/cm² [11]. (b) 7×10^{13} W/cm². (c) 4×10^{13} W/cm². (d) Longitudinal momentum distribution of Ar²⁺ ions at 7×10^{13} W/cm².

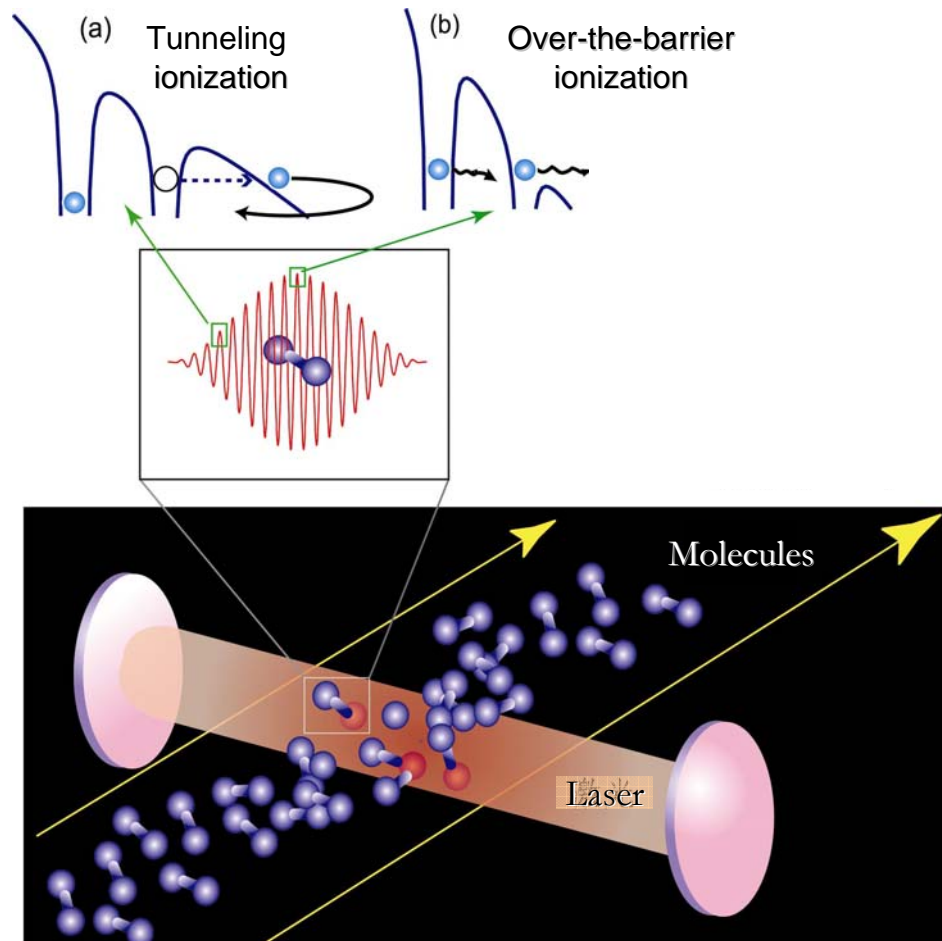
Theoretical Dificulties



- 1. Perturbation theory
The laser field has reached or even exceeded the Coulomb attraction 
- 2. 3D quantum calculation
Far exceed the capability even of the best computer 
- 3. 1D quantum calculation
Do not include effects such as Coulomb focusing 
- 4. Classical MC calculation
Do not include effects such as quantum tunneling 
- S-Matrix, Floque theory

Semiclassical model

(Phys.Rev.Lett. 99, 013003, 2007)



Overview

The model is based upon the **rescattering picture**

It has included all the effects that determine the DI process

quantum tunneling

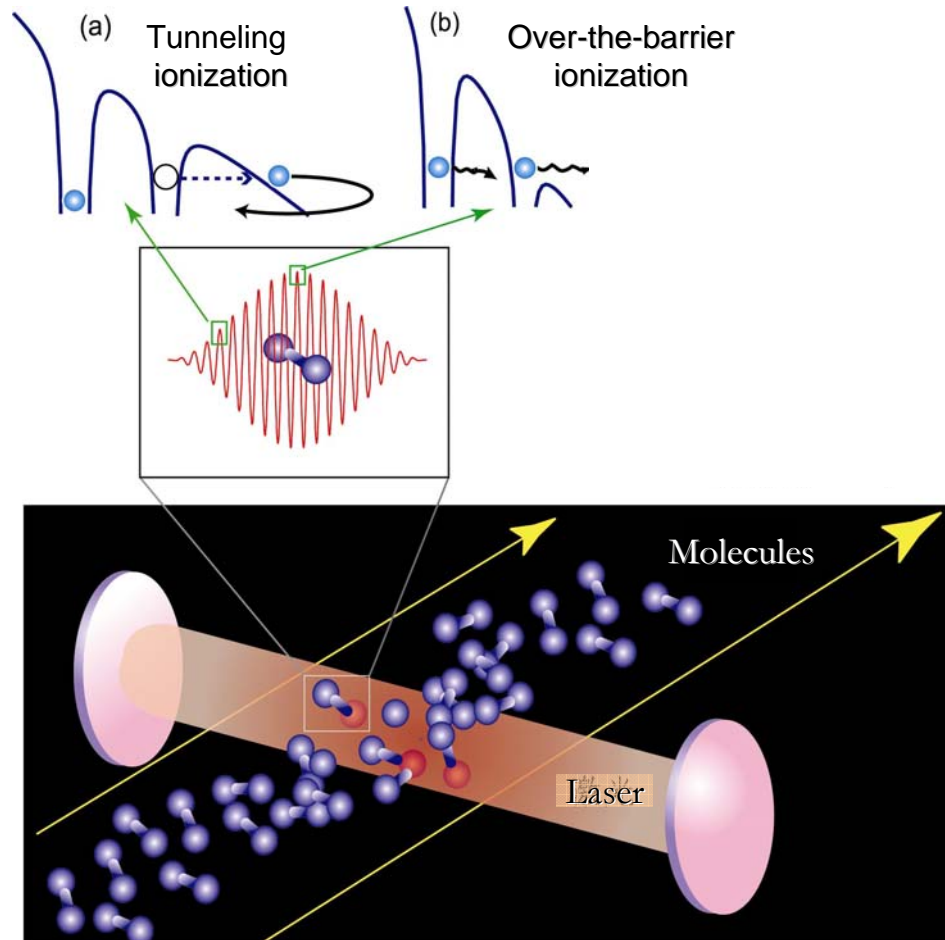
Coulomb focusing

.....

while keeps the **computational capacity** still accessible.

The dynamics of two electrons are governed by **Newton's equations**.

Semiclassical model ... continued



Newton's equation

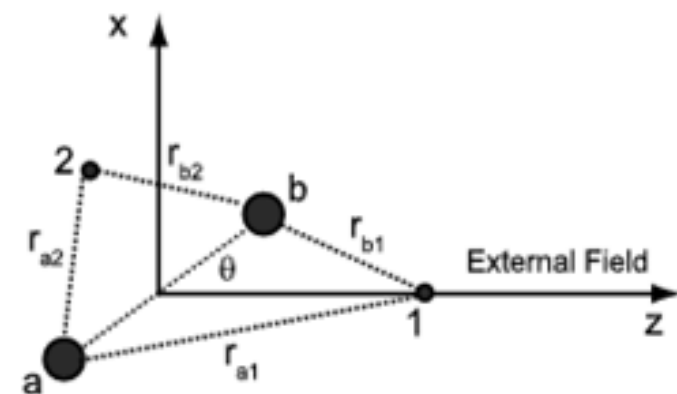
$$\frac{d^2 \mathbf{r}_i}{dt^2} = \mathbf{E}(t) - \nabla(V_{ne} + V_{ee})$$

$$\mathbf{E}(t) = (\varepsilon(t) \sin \theta, 0, \varepsilon(t) \cos \theta)$$

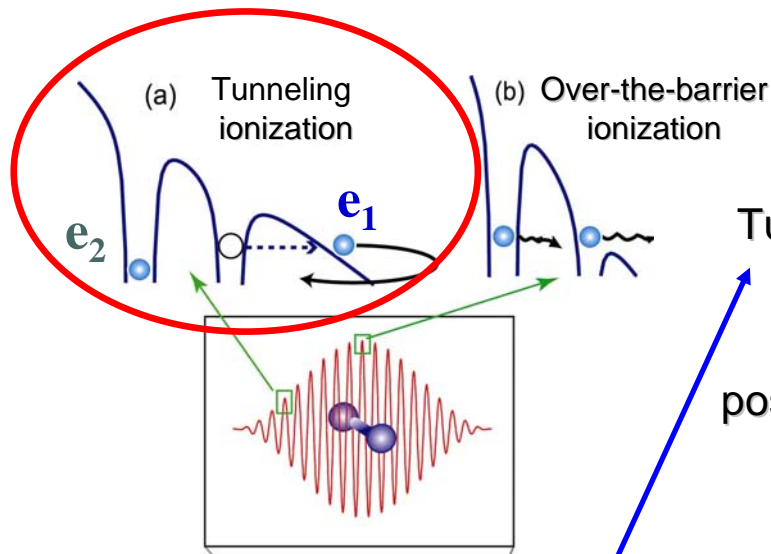
$$\varepsilon(t) = \varepsilon \cos(\omega t).$$

$$V_{ne}^i = -\frac{Z_{eff}}{r_{at}} - \frac{Z_{eff}}{r_{bt}};$$

$$V_{ee} = \frac{1}{|\mathbf{r}_1 - \mathbf{r}_2|}.$$



Semiclassical model ... continued



Initial distribution

(a) Tunneling regime

Tunneled electron e_1

$$\text{position} \begin{cases} -\frac{1}{r_{a1}} - \frac{1}{r_{b1}} + \int \frac{|\Psi(\mathbf{r}')|^2}{|\mathbf{r}_1 - \mathbf{r}'|} d\mathbf{r}' + I_{p1} - z_1 \varepsilon(t_0) = 0, \\ x_1 = y_1 = 0 \end{cases}$$

$$\text{momentum} \begin{cases} (v_{\perp} \cos \varphi, v_{\perp} \sin \varphi, 0) \\ w(v_{\perp}) dv_{\perp} = \frac{2(2I_{p1})^{1/2} v_{\perp}}{\varepsilon(t_0)} \exp\left(-\frac{v_{\perp}^2 (2I_{p1})^{1/2}}{\varepsilon(t_0)}\right) dv_{\perp} \end{cases}$$

Bound electron e_2

Single electron Microcanonical Distribution (SMD)

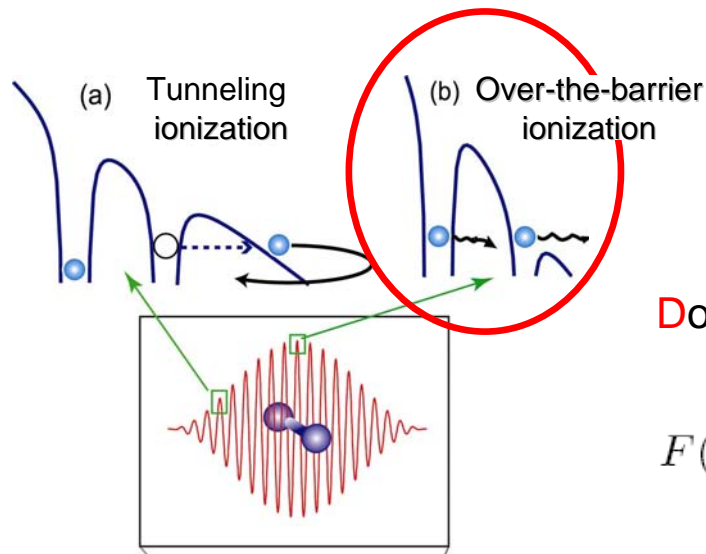
$$\text{position} \begin{cases} F(\mathbf{r}_2, \mathbf{p}_2) = k\delta[I_{p2} - \mathbf{p}_2^2/2 - W(r_{a2}, r_{b2})]. \end{cases}$$

+

$$\text{momentum} \begin{cases} W(r_{a2}, r_{b2}) = -1/r_{a2} - 1/r_{b2} \end{cases}$$

J. Chen, J. Liu, L. B. Fu, and W. M. Zheng Phys. Rev. A **63**, 011404(R) (2000); Li-Bin Fu, Jie Liu, Jing Chen, and Shi-Gang Chen Phys. Rev. A **63**, 043416 (2001); Li-Bin Fu, Jie Liu, and Shi-Gang Chen Phys. Rev. A **65**, 021406(R) (2002); J. Chen, J. Liu, and W. M. Zheng Phys. Rev. A **66**, 043410 (2002).

R. Abrines and LC. Percival, Proc. Phys. Soc. London **88**, 861 (1966); J. G. Leopold and I. C. Percival, J. Phys. B **12**, 709 (1979).



Initial distribution

(b) Over-the-barrier regime

Double electron **M**icrocanonical **D**istribution (DMD)

$$F(\mathbf{r}_1, \mathbf{r}_2, \mathbf{p}_1, \mathbf{p}_2) = \frac{1}{2} [f_\alpha(\mathbf{r}_1, \mathbf{p}_1) f_\beta(\mathbf{r}_2, \mathbf{p}_2) + f_\beta(\mathbf{r}_1, \mathbf{p}_1) f_\alpha(\mathbf{r}_2, \mathbf{p}_2)],$$

$$f_{\alpha,\beta}(\mathbf{r}, \mathbf{p}) = k\delta\left[I_{p1} - \frac{\mathbf{p}^2}{2} - W(r_a, r_b) - V_{\alpha,\beta}(\mathbf{r})\right],$$

$$V_{\alpha,\beta}^*(\mathbf{r}) = \frac{1}{r_{b,a}} [1 - (1 + \kappa r_{b,a}) e^{-2\kappa r_{b,a}}].$$

L. Meng, C. O. Reinhold and R. E. Olson, Phys. Rev. A **40**, 3637 (1989).

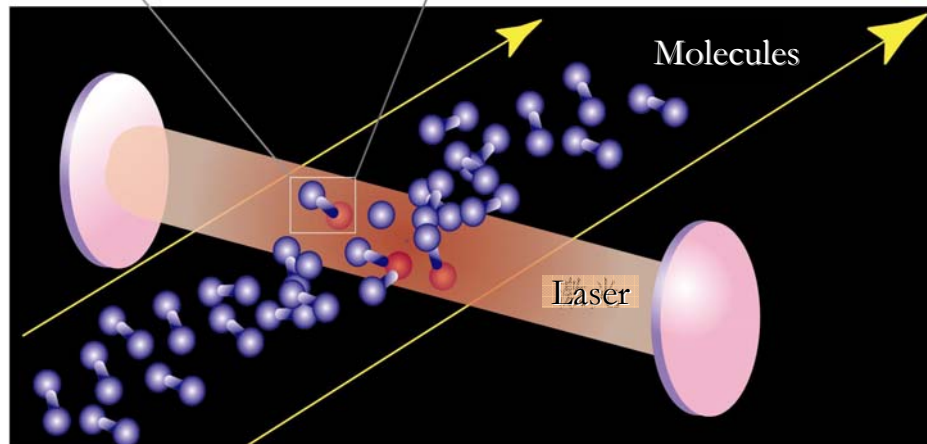
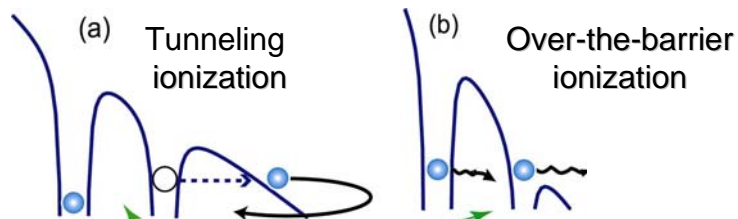
Semiclassical model ... continued



Each event has different weight →

molecular ADK formula:

$$w(0) = \frac{16 \cdot c_1^2 (2I_{p1})^{5/2}}{\epsilon^2} e^{-\kappa R} \int_0^{2\pi} d\phi \int_0^1 \frac{\cosh^2\left(\frac{\kappa R \mu}{2}\right)}{\mu d\mu} \frac{1}{[\sin \theta \cos \phi (1 - \mu^2)^{1/2} + \mu \cos \theta]^2} \times \exp\left[-\frac{2}{3\epsilon} \frac{(I_{p1})^{3/2}}{\sin \theta \cos \phi (1 - \mu^2)^{1/2} + \mu \cos \theta}\right]$$

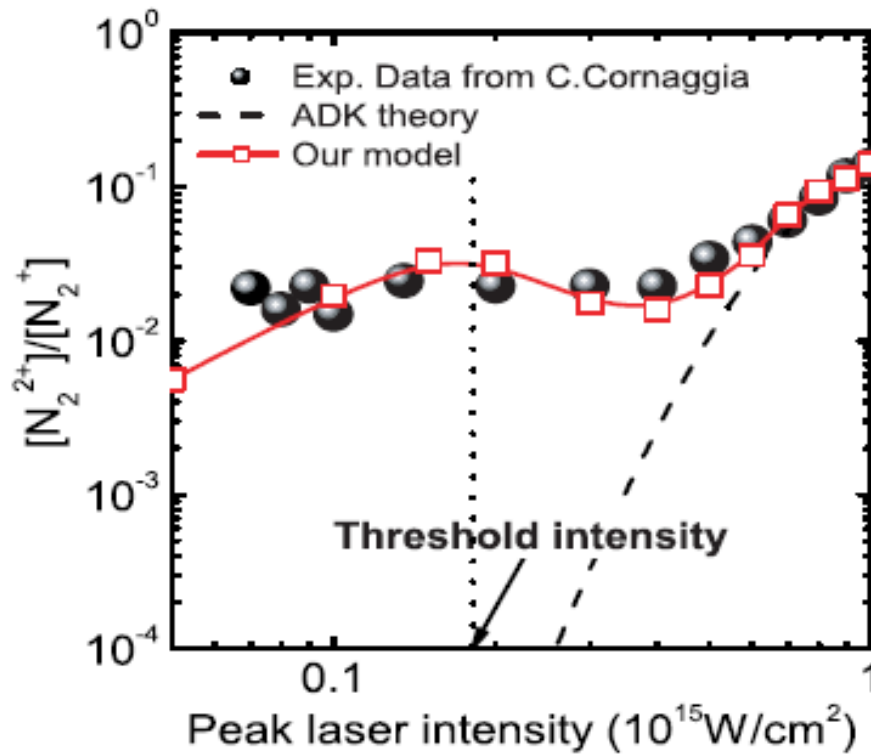


NOTE: The total ionization rate should be summed over the

- pulse duration
- interaction volume
- alignment angle

in order to compare with the experimental data.

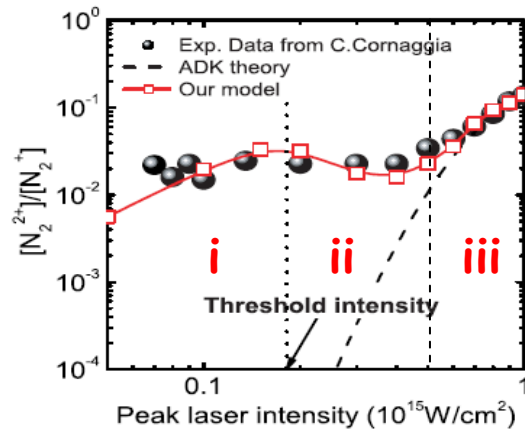
First sight of the model calculation



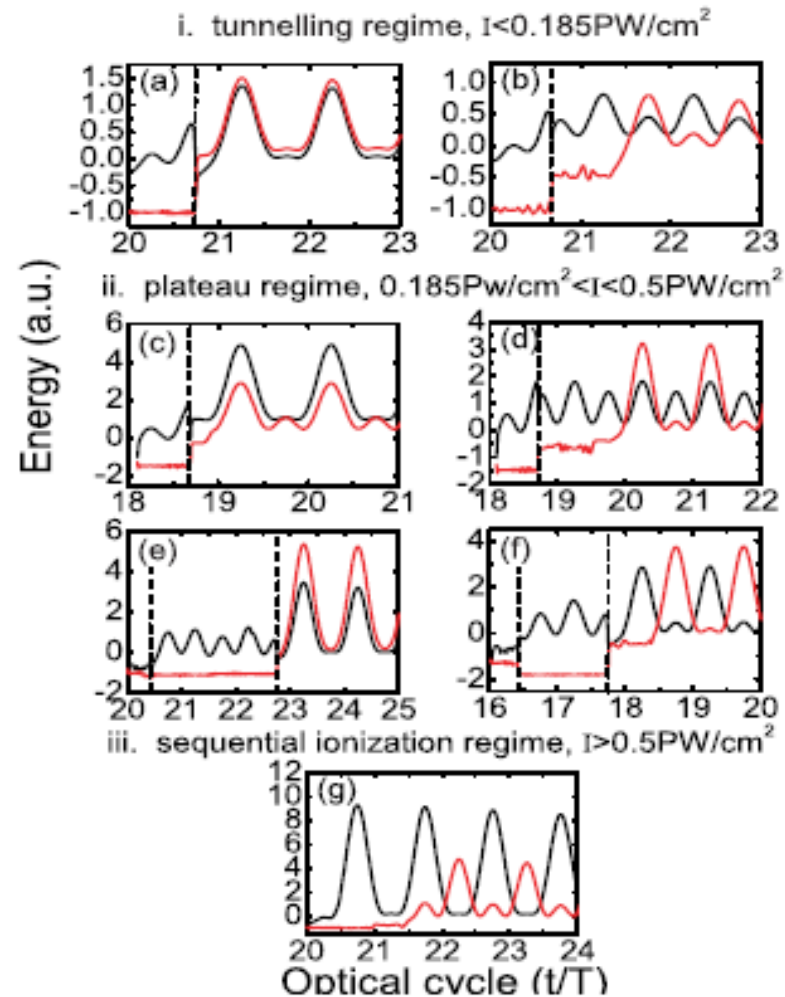
Good Agreement!

C. Cornaggia and Ph.Hering
Phys. Rev. A 62, 023403 (2000)

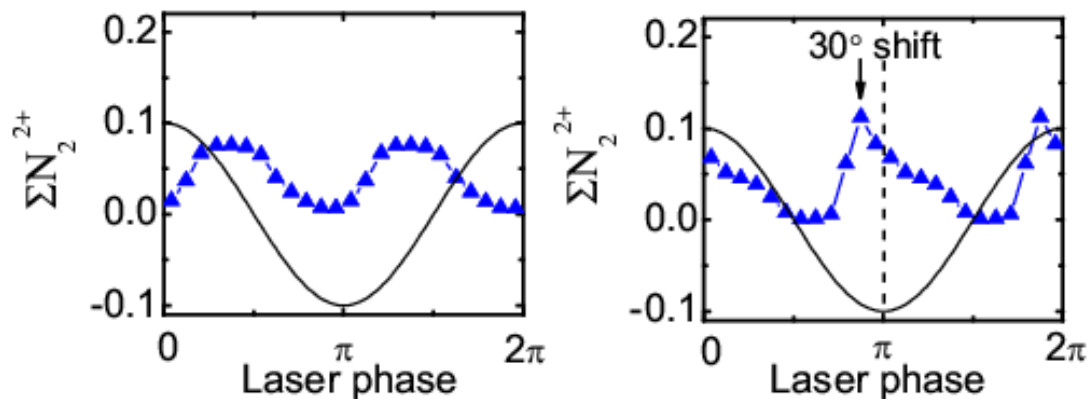
Subcycle dynamics



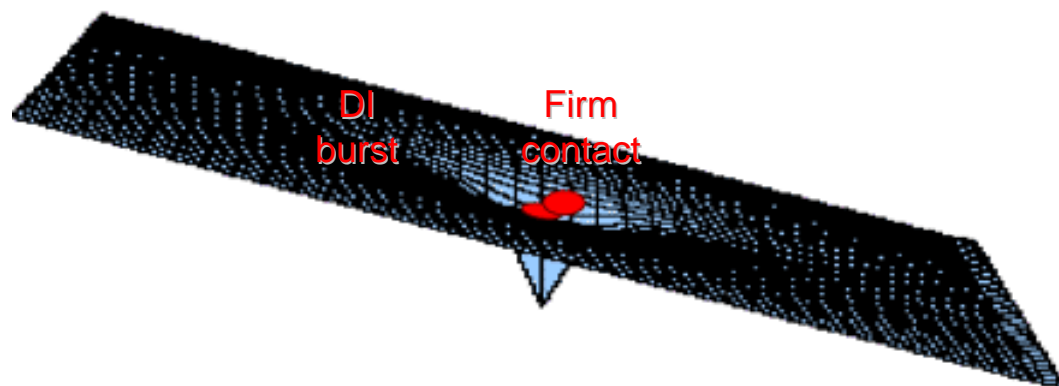
- (i) **Tunneling regime:**
collision-ionization (CI)
collision-excitation-ionization (CEI)
- (ii) **Plateau regime:**
trajectories are much more complicated.
multiple-collision trajectories
- (iii) **Sequential ionization regime:**
ionize independently



Laser phase: at firm contact & DI burst



Most electron pairs recollide at the **laser zero**, that is because when the returned electrons come back at this time, it obtain the **largest kinetic energy**, thus would cause double ionization more **easily**.



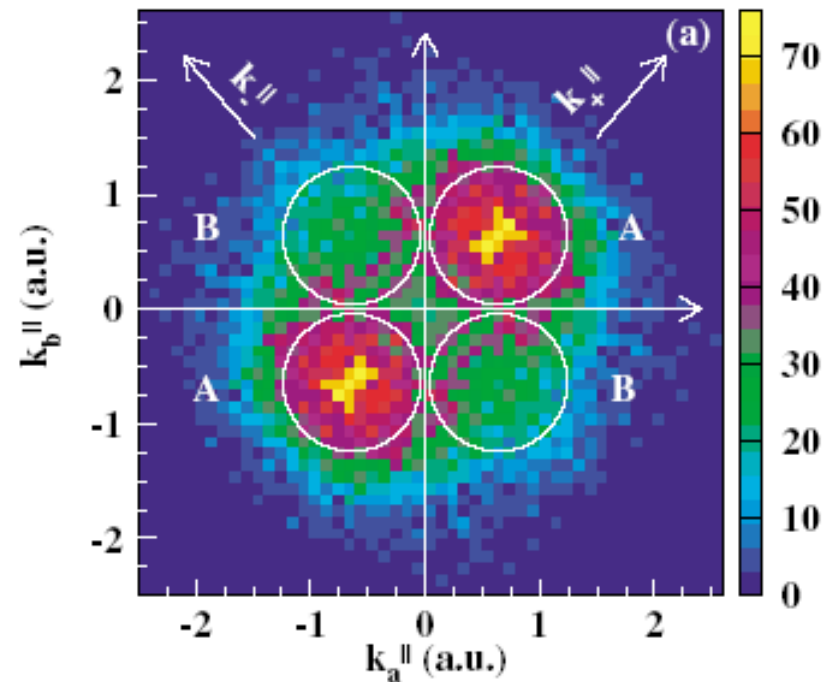
DI occurs a little later, about **30° before** the laser peak, leading to the emission of electron pairs with nonzero momentum and in the same direction (**e-e correlation**), see next slide.

Two most important instant



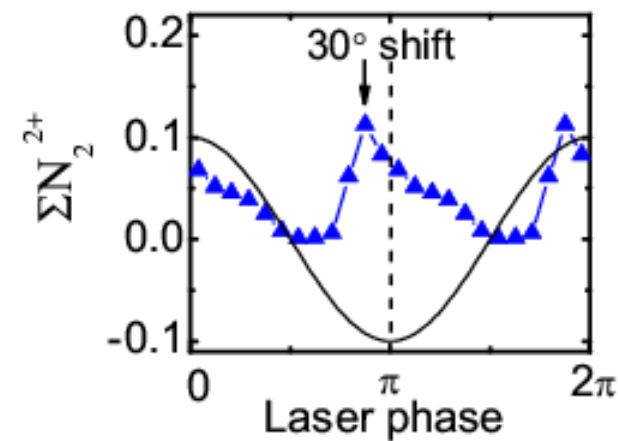
Fully Differential Rates for Femtosecond Multiphoton Double Ionization of Neon

M. Weckenbrock,¹ D. Zeidler,² A. Staudte,¹ Th. Weber,¹ M. Schöffler,¹ M. Meckel,¹ S. Kammer,¹ M. Smolarski,¹
O. Jagutzki,¹ V.R. Bhardwaj,² D.M. Rayner,² D.M. Villeneuve,² P.B. Corkum,² and R. Dörner^{1,*}

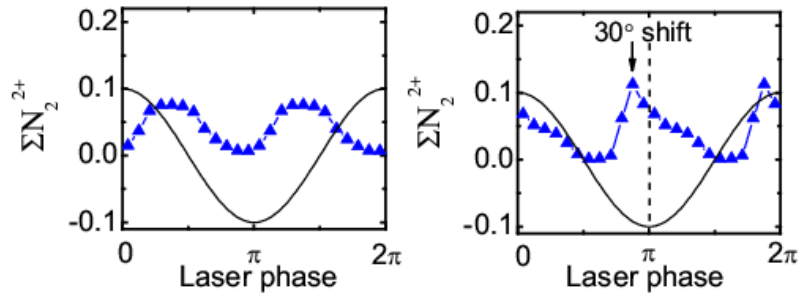


argon [23]). We also find that the two electrons often have similar momentum in the direction parallel to the laser field. Assuming that this momentum is primarily obtained from the laser field, we deduce that both electrons are reemitted at about **30° before or after** the maximum of the laser field. Electrons that have similar

$$k_{a,b}^{\parallel} = 2\sqrt{U_p} \sin\omega t_{\text{ion}}.$$



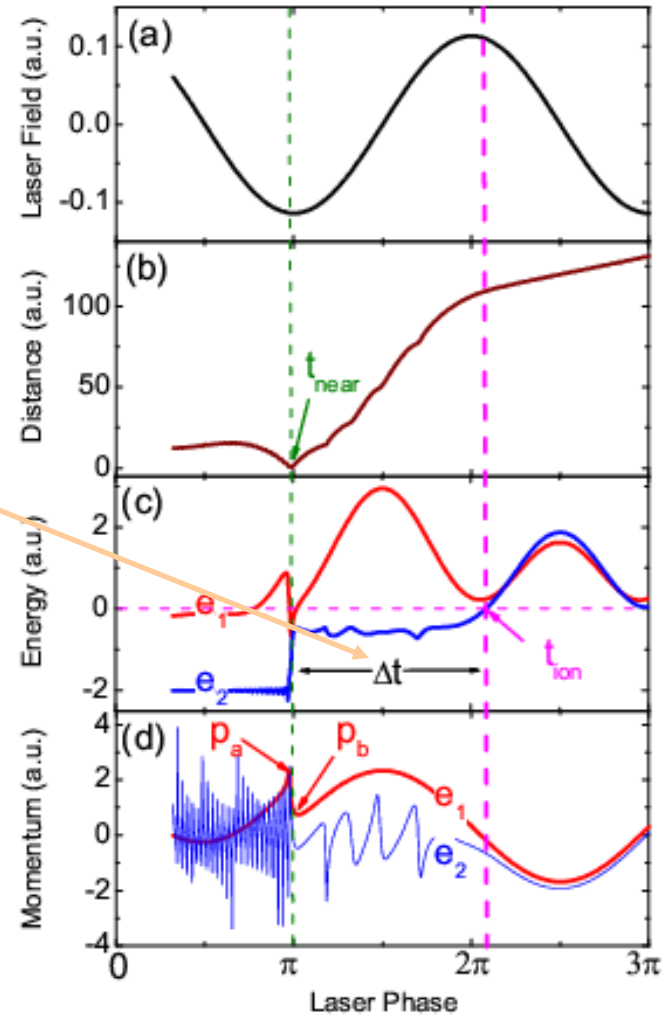
Time delay



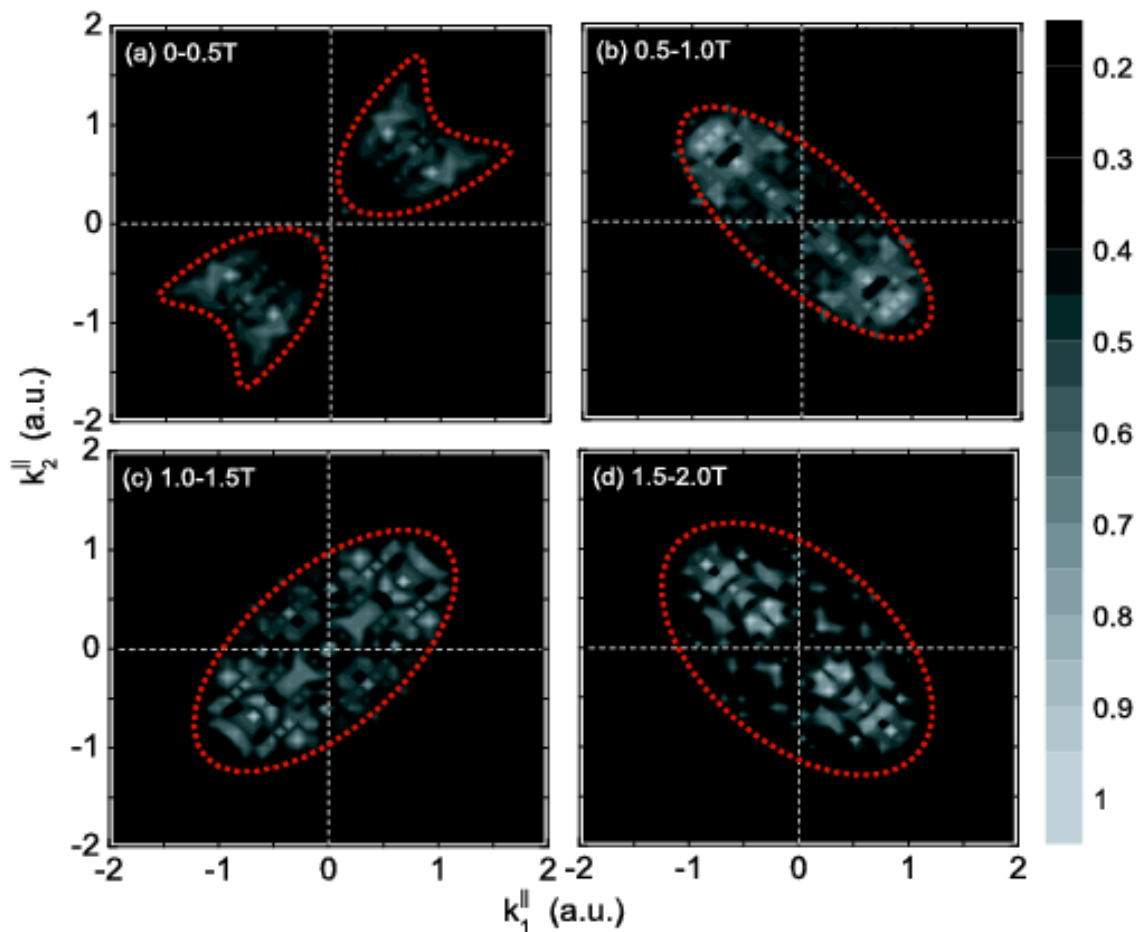
Time Delay

Time delay between double ionization and recollision

1. Statistical result
2. Individual trajectory
3. Effects on the DI dynamics



Momentum correlation: time delay effect



Momentum distributions with certain time delays.

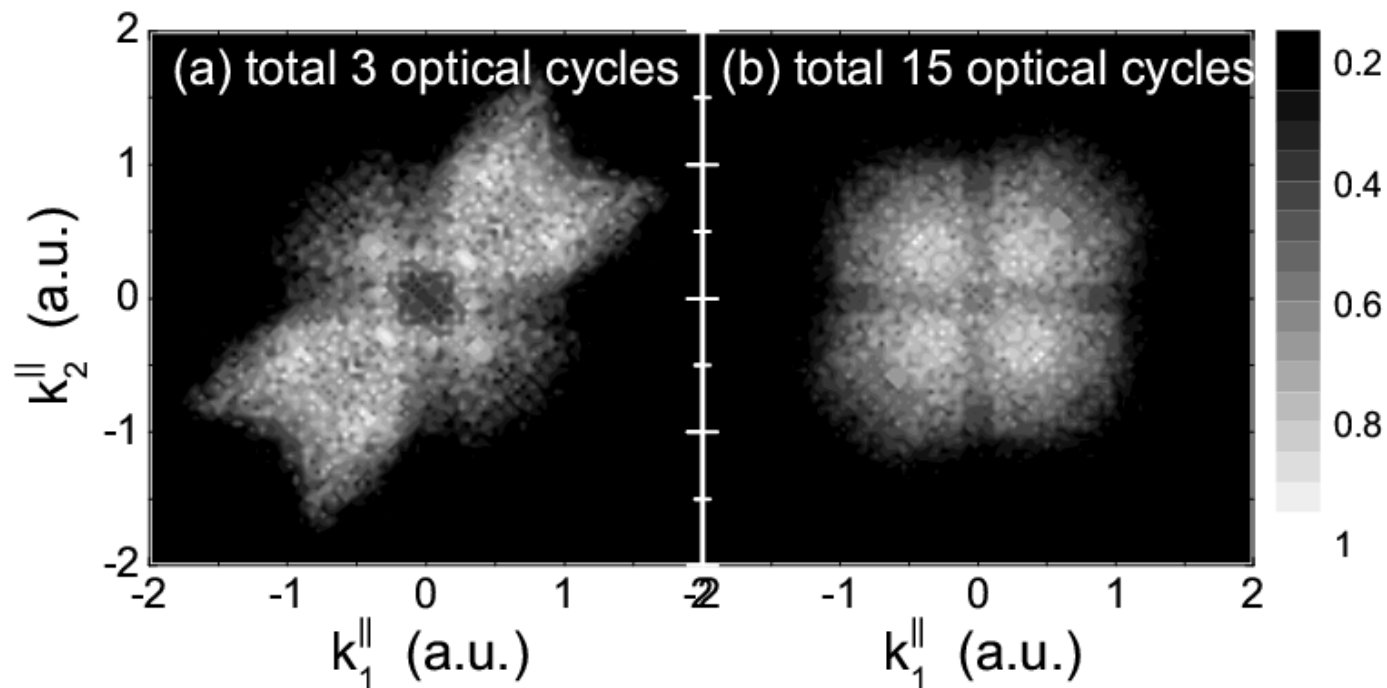
- (a) (c) time delay of odd half laser cycles, same hemisphere emission

(b) (d) time delay of even half laser cycles, opposite hemisphere emission
- (a) fingerlike pattern

(b)-(d) elliptical pattern
- As the time delay increase the elliptical pattern becomes fatter and fatter, indicating the vanish of correlation between two electrons.

Phys.Rev.A. 77, 013403, 2008

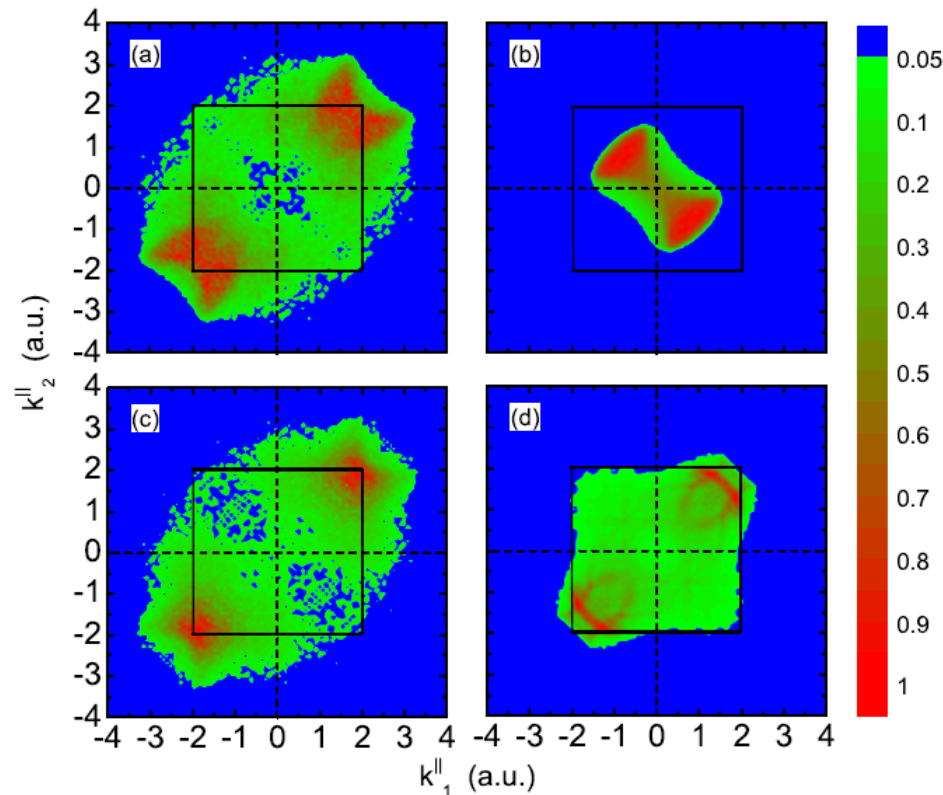
Momentum correlation: laser duration effect



Shorter laser pulse, fingerlike pattern is more **pronounced**

Longer laser pulse, correlation become **blurry**

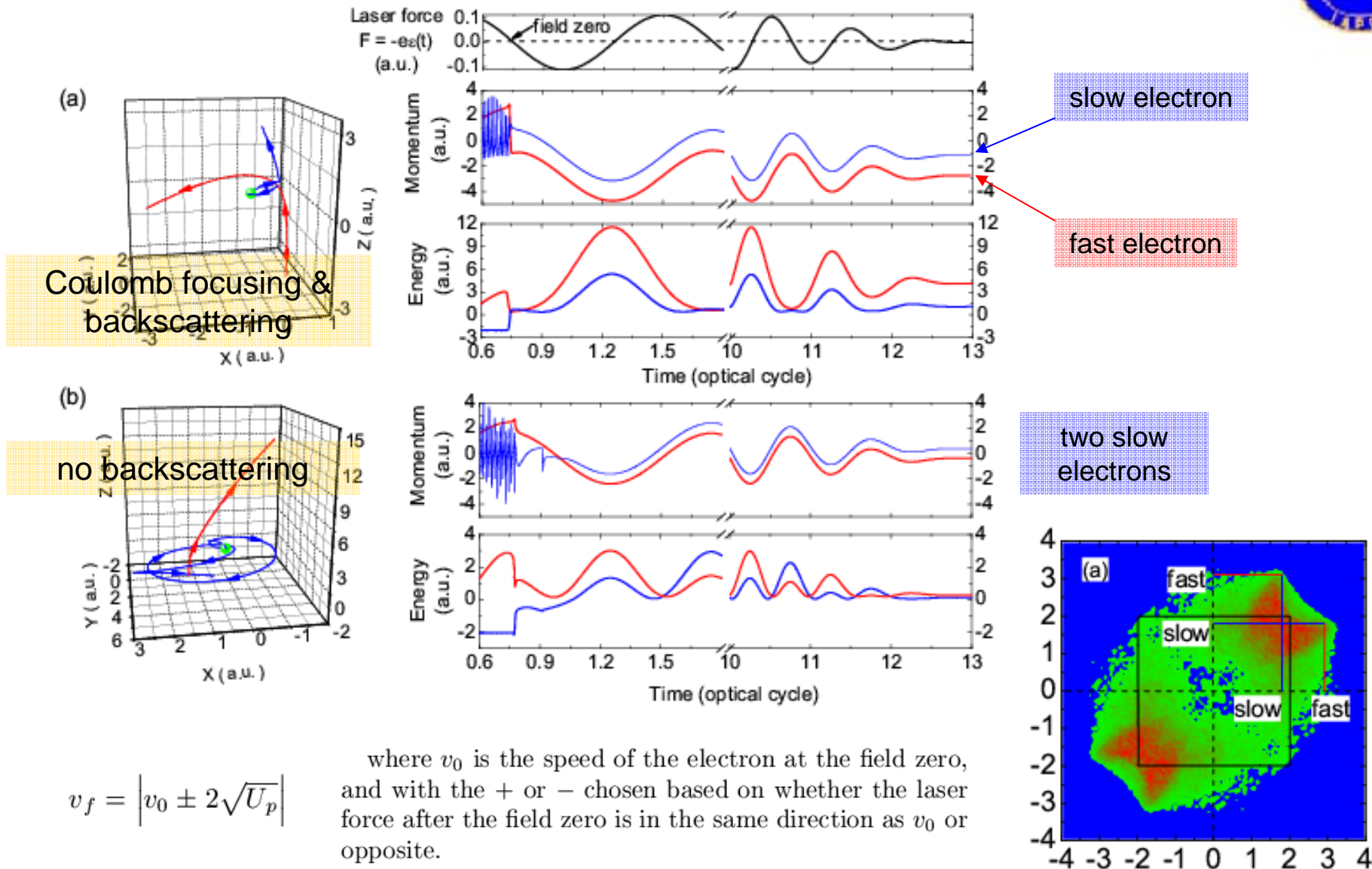
Why finger structure (or V-shaped)? (1)



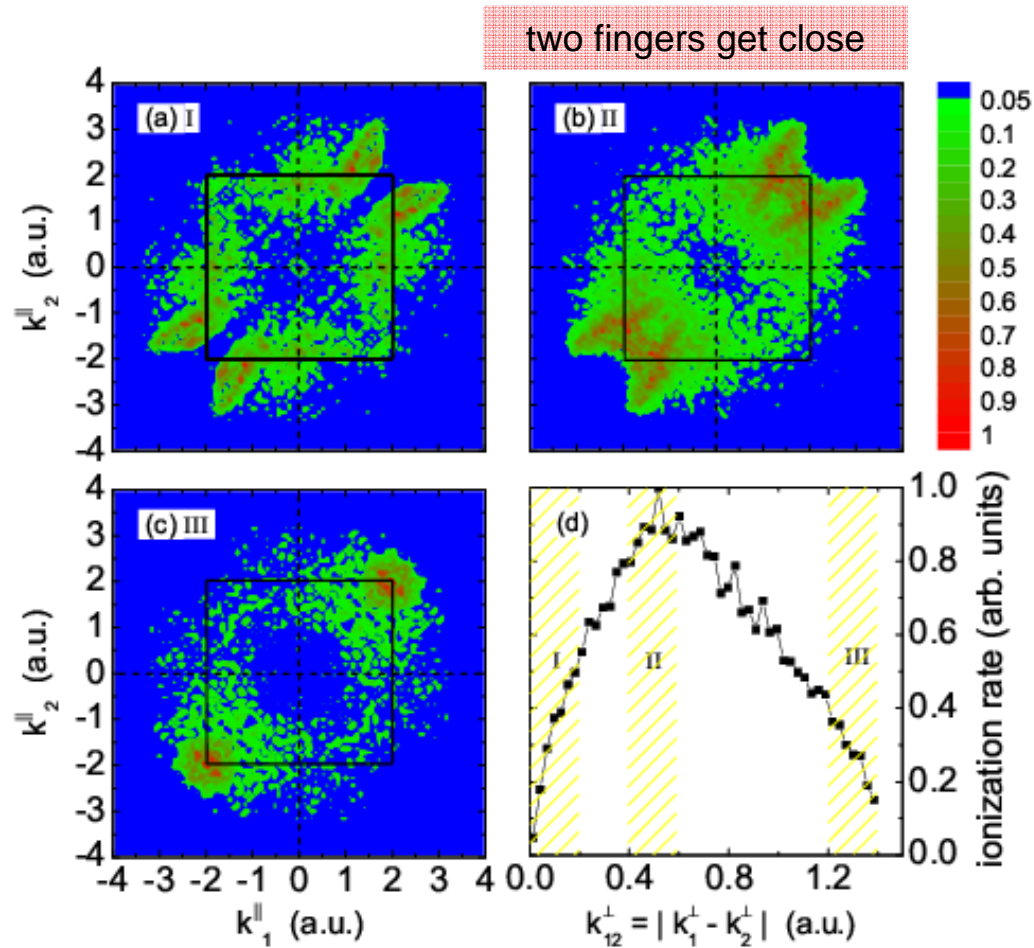
(a) Distribution of correlated electron momenta along the laser polarization for Helium DI irradiated by 800nm, $4.5 \times 10^{14} \text{W/cm}^2$ laser pulses. The black box indicates the $2\sqrt{U_p}$ boundary of electron momentum. The model calculations under various circumstances yield very different momentum distribution patterns(see text for details): (b) the laser field is removed and the tunneled electrons are replaced by a beam of projectile electrons; (c) the electron-electron Coulombic interaction is replaced with a Yukawa potential; (d) the nuclear Coulomb potential is softened.

The Coulomb-type attraction of nucleus is especially important for the production of fingerlike structure

Why finger structure (or V-shaped)? (2)

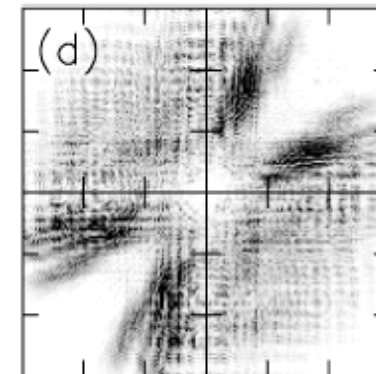


Perpendicular effect



Correlated parallel momentum distributions with additional conditions on the relative perpendicular momentum between two electrons, i.e., for (a) $0 \leq k_{12}^{\perp} \leq 0.2$, (b) $0.4 \leq k_{12}^{\perp} \leq 0.6$, (c) $1.2 \leq k_{12}^{\perp} \leq 1.4$. (d) The overall relative perpendicular momentum distribution.

1D quantum calculation



two fingers disappear

Conclusion



1. Set up a semiclassical model for the double ionization problem.

Advantages:

- ☆ Include most of the important effects in DI process, e.g. the quantum tunneling and the Coulomb focusing.
 - ☆ Underlying mechanisms can be identified with the Classical Trajectory (CT) diagnosis
2. Reproduce and explain many experimental observations.
 - ☆ DI ratio
 - ☆ Finger-like structure
 -

Thank You